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{- $Id: AFRP.hs,v 1.14 2002/04/30 23:29:46 henrik Exp $
*****
*
*           A F R P
*
*   Module:      AFRP
*   Purpose:     The AFRP core.
*   Authors:    Antony Courtney and Henrik Nilsson
*
*****
-}

module AFRP (
-- Re-exported modules
  module Arrow,
  module AFRPTuple, -- Utility functions and numeric instances for tuples.

-- Main types
  Time, -- [s] Both for time w.r.t. some reference and intervals.
  SF, -- Signal Function.
  Event, -- Events; conceptually similar to Maybe (but abstract).

-- Main instances
  -- SF is an instance of Arrow and ArrowLoop. Method instances:
  -- arr :: (a -> b) -> SF a b
  -- (>>>) :: SF a b -> SF b c -> SF a c
  -- first :: SF a b -> SF (a,c) (b,c)
  -- second :: SF a b -> SF (c,a) (c,b)
  -- (***) :: SF a b -> SF a' b' -> SF (a,a') (b,b')
  -- (&&&) :: SF a b -> SF a b' -> SF a (b,b')
  -- returnA :: SF a a
  -- loop :: SF (a,c) (b,c) -> SF a b

  -- Event is an instance of Functor, Eq, and Ord. Some method instances:
  -- fmap :: (a -> b) -> Event a -> Event b
  -- (==) :: Event a -> Event a -> Bool
  -- (<=) :: Event a -> Event a -> Bool

-- Basic signal functions
  identity, -- :: SF a a
  constant, -- :: b -> SF a b
  localTime, -- :: SF a Time
  time, -- :: SF a Time

-- Initialization
  initially, -- :: a -> SF a a

-- Basic event sources
  never, -- :: SF a (Event b)
  now, -- :: b -> SF a (Event b)
  snap, -- :: SF a (Event a)
  after, -- :: Time -> b -> SF a (Event b)
  repeatedly, -- :: Time -> b -> SF a (Event b)
  edge, -- :: SF Bool (Event ())
  edgeJust, -- :: SF (Maybe a) (Event a)
  edgeBy, -- :: (a -> a -> Maybe b) -> a -> SF a (Event b)

-- Stateful event suppression
  notYet, -- :: SF (Event a) (Event a)

-- Collection-oriented combinators
  par, -- :: Functor col => col (SF a b) -> SF a (col b)

-- Switchers
  switch, dSwitch, -- :: SF a (b, Event c) -> (c -> SF a b) -> SF a b
  kSwitch, dkSwitch, -- :: SF a b
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-- -> SF (a,b) (Event c)
-- -> (SF a b -> c -> SF a b)
-- -> SF a b
rSwitch, drSwitch, -- :: SF a b -> SF (a,Event (SF a b)) b
pSwitch, dpSwitch, -- :: Functor col =>
  col (SF a b)
  -> SF (a, col b) (Event c)
  -> (col (SF a b) -> c -> SF a (col b))
  -> SF a (col b)
rpSwitch, drpSwitch, -- :: Functor col =>
  col (SF a b)
  -> SF (a, Event (col (SF a b)->col (SF a b)))
  (col b)

-- Wave-form generation
  hold, -- :: a -> SF (Event a) a
  dHold, -- :: a -> SF (Event a) a
  trackAndHold, -- :: a -> SF (Maybe a) a
  dTrackAndHold, -- :: a -> SF (Maybe a) a

-- Accumulators
  accum, -- :: a -> SF (Event (a -> a)) (Event a)
  accumBy, -- :: (b -> a -> b) -> b -> SF (Event a) (Event b)
  accumFilter, -- :: (c -> a -> (c, Maybe b)) -> c
  -- -> SF (Event a) (Event b)
  count, -- :: Integral b => SF (Event a) (Event b)

-- Delay
  delay, -- :: a -> SF a a

-- Integral
  integral, -- :: Fractional a => SF a a

-- Loops with guaranteed well-defined feedback
  loopDelay, -- :: c -> SF (a,c) (b,c) -> SF a b
  loopIntegral, -- :: Fractional c => SF (a,c) (b,c) -> SF a b

-- Pointwise functions on events
  event, -- :: a -> (b -> a) -> Event b -> a
  fromEvent, -- :: Event a -> a
  isEvent, -- :: Event a -> Bool
  isNoEvent, -- :: Event a -> Bool
  tag, -- :: Event a -> b -> Event b
  lMerge, -- :: Event a -> Event a -> Event a
  rMerge, -- :: Event a -> Event a -> Event a
  merge, -- :: Event a -> Event a -> Event a
  mergeBy, -- :: (a -> a -> a) -> Event a -> Event a -> Event a
  mergeEvents, -- :: [Event a] -> Event a
  joinE, -- :: Event a -> Event b -> Event (a,b)
  filterE, -- :: (a -> Bool) -> Event a -> Event a
  gateE, -- :: Bool -> Event a -> Event a

-- Reactimation
  reactimate, -- :: IO a
  -- -> (Bool -> IO (DTime, Maybe a))
  -- -> (Bool -> b -> IO Bool)
  -- -> SF a b
  -- -> IO ()

-- Embedding (tentative: will be revisited)
  DTime, -- [s] Sampling interval, always > 0.
  embed, -- :: SF a b -> (a, [(DTime, Maybe a)]) -> [b]
  deltaEncode, -- :: Eq a => DTime -> [a] -> (a, [(DTime, Maybe a)])
  deltaEncodeBy, -- :: (a -> a -> Bool) -> DTime -> [a]
  -- -> (a, [(DTime, Maybe a)])
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AFRP.hs

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) where

import Monad (unless)

import Arrow
import AFRPDiagnostics
import AFRPTuple
import AFRPEvent

-----
-- Basic type definitions with associated utilities
-----

-- The time type is really a bit boguous, since, as time passes, the minimal
-- interval between two consecutive floating-point-represented time points
-- increases. A better approach is probably to pick a reasonable resolution
-- and represent time and time intervals by Integer (giving the number of
-- "ticks").

-- Time is used both for time intervals (duration), and time w.r.t. some
-- agreed reference point in time. Conceptually, Time = R, i.e. time can be 0
-- or even negative.
type Time = Double    -- [s]

-- DTime is the time type for lengths of sample intervals. Conceptually,
-- DTime = R+ = { x in R | x > 0 }. Don't assume Time and DTime have the
-- same representation.

type DTime = Double   -- [s]

-- Representation of signal function in initial state.
-- (Naming: "TF" stands for Transition Function.)

data SF a b = SF {sfTF :: a -> Transition a b}

-- Representation of signal function in running state.
-- It would have been nice to have a constructor SFId representing (arr id):
--
--     SFId {sfTF' :: DTime -> a -> Transition a b}
--
-- But it seems as if we need dependent types as soon as we try to exploit
-- that constructor (note that the type above is too general!), and a
-- work-around based on keeping around an extra function as a "proof" that we
-- can do the required coersions, yields code which is no more efficient
-- than using SFArr in the first place.
-- (Naming: "TIVar" stands for "time-input-variable".)

data SF' a b
  = SFConst {sfTF' :: DTime -> a -> Transition a b, sfCVal :: b}
  | SFArr   {sfTF' :: DTime -> a -> Transition a b, sfAFun :: a -> b}
  | SFTIVar {sfTF' :: DTime -> a -> Transition a b}

-- A transition is a pair of the next state (in the form of a signal
-- function) and the output at the present time step.

type Transition a b = (SF' a b, b)

-- "Smart" constructors. The corresponding "raw" constructors should not
-- be used directly for construction.

sfConst :: b -> SF' a b
sfConst b = sf
  where
    sf = SFConst {sfTF' = \_ _ -> (sf, b), sfCVal = b}

-- !!! We could/should use NeverEvent here!
sfNever :: SF' a (Event b)
sfNever = sfConst NoEvent

sfId :: SF' a a
sfId = sf
  where
    sf = SFArr {sfTF' = \_ a -> (sf, a), sfAFun = id}

sfArr :: (a -> b) -> SF' a b
sfArr f = sf
  where
    sf = SFArr {sfTF' = \_ a -> (sf, f a), sfAFun = f}

-- Freezes a "running" signal function, i.e., turns it into a continuation in
-- the form of a plain signal function.
freeze :: SF' a b -> DTime -> SF a b
freeze sf dt = SF {sfTF = (sfTF' sf) dt}

freezeCol :: Functor col => col (SF' a b) -> DTime -> col (SF a b)
freezeCol sfs dt = fmap (flip freeze dt) sfs

-----
-- Arrow instance and implementation
-----

instance Arrow SF where
  arr      = arrPrim
  (>>>)   = compPrim
  first    = firstPrim
  second   = secondPrim

-- Lifting.
arrPrim :: (a -> b) -> SF a b
arrPrim f = SF {sfTF = \a -> (sfArr f, f a)}

-- Composition.
-- The definition exploits the following identities:
--     sf >>> constant c = constant c
--     constant c >>> arr f = constant (f c)
--     arr f >>> arr g = arr (g . f)
-- (It would have been nice to explit e.g. identity >>> sf = sf, but it would
-- seem that we need dependent types for that.)
compPrim :: SF a b -> SF b c -> SF a c
compPrim (SF {sfTF = tf10}) (SF {sfTF = tf20}) = SF {sfTF = tf0}
  where
    tf0 a0 = (cpAux sf1 sf2, c0)
      where
        (sf1, b0) = tf10 a0
        (sf2, c0) = tf20 b0

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cpAux sf1      sf2@(SFConst{}) = sfConst (sfCVal sf2)
cpAux sf1@(SFConst{}) sf2@(SFArr {}) = sfConst (sfAFun sf2
                                                (sfCVal sf1))
cpAux sf1@(SFArr {}) sf2@(SFArr {}) = sfArr (sfAFun sf2 . sfAFun sf1)
cpAux sf1      sf2      = SFTIVar {sfTF' = tf}
  where
    tf dt a = (cpAux sf1' sf2', c)
              where
                (sf1', b) = (sfTF' sf1) dt a
                (sf2', c) = (sfTF' sf2) dt b

-- Widening.
-- The definition exploits the following identities:
-- first (constant b) = arr (\(_, c) -> (b, c))
-- (first (arr f))    = arr (\(a, c) -> (f a, c))
-- (It would have been nice to explit first identity = identity, but it would
-- seem that we need dependent types for that.)
firstPrim :: SF a b -> SF (a,c) (b,c)
firstPrim (SF {sfTF = tf10}) = SF {sfTF = tf0}
  where
    tf0 (a0, c0) = (fpAux sf1, (b0, c0))
              where
                (sf1, b0) = tf10 a0

    fpAux (SFConst {sfCVal = b}) = sfArr (\(_, c) -> (b, c))
    fpAux (SFArr {sfAFun = f}) = sfArr (\(a, c) -> (f a, c))
    fpAux sf1 = SFTIVar {sfTF' = tf}
      where
        tf dt (a, c) = (fpAux sf1', (b, c))
                      where
                        (sf1', b) = (sfTF' sf1) dt a

secondPrim :: SF a b -> SF (c,a) (c,b)
secondPrim (SF {sfTF = tf10}) = SF {sfTF = tf0}
  where
    tf0 (c0, a0) = (spAux sf1, (c0, b0))
              where
                (sf1, b0) = tf10 a0

    spAux (SFConst {sfCVal = b}) = sfArr (\(c, _) -> (c, b))
    spAux (SFArr {sfAFun = f}) = sfArr (\(c, a) -> (c, f a))
    spAux sf1 = SFTIVar {sfTF' = tf}
      where
        tf dt (c, a) = (spAux sf1', (c, b))
                      where
                        (sf1', b) = (sfTF' sf1) dt a

-----
-- ArrowLoop instance and implementation
-----

instance ArrowLoop SF where
  loop = loopPrim

loopPrim :: SF (a,c) (b,c) -> SF a b
loopPrim (SF {sfTF = tf10}) = SF {sfTF = tf0}
  where
    tf0 a0 = (loopAux sf1, b0)
            where
              (sf1, (b0, c0)) = tf10 (a0, c0)

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loopAux (SFConst {sfCVal = (b, _)}) = sfConst b
loopAux sf1 = SFTIVar {sfTF' = tf}
  where
    tf dt a = (loopAux sf1', b)
              where
                (sf1', (b, c)) = (sfTF' sf1) dt (a, c)

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-----
-- Basic signal functions
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-- Identity: identity = arr id
identity :: SF a a
identity = SF {sfTF = \a -> (sfId, a)}

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-- Identity: constant b = arr (const b)
constant :: b -> SF a b
constant b = SF {sfTF = \_ -> (sfConst b, b)}

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-- Outputs the time passed since the signal function instance was started.
localTime :: SF a Time
localTime = constant 1.0 >>> integral

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-- Alternative name for localTime.
time :: SF a Time
time = localTime

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-- Initialization
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-- The identity function, except at (local) time 0 where the initial value is
-- output instead.
initially :: a -> SF a a
initially a_init = SF {sfTF = \_ -> (sfId, a_init)}

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-- Basic event sources
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-- Event source which never occurs.
-- !!! We could/should use NeverEvent here.
never :: SF a (Event b)
never = SF {sfTF = \_ -> (sfNever, NoEvent)}

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-- Event source with a single occurrence at time 0. The value of the event
-- is given by the function argument.
now :: b -> SF a (Event b)
now b0 = SF {sfTF = \_ -> (sfNever, Event b0)}

```

```

-- Event source with a single occurrence at time 0. The value of the event
-- is obtained by sampling the input at that time.
snap :: SF a (Event a)
snap = SF {sfTF = \a0 -> (sfNever, Event a0)}

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-- Event source with a single occurrence at or as soon after (local) time t_ev
-- as possible.
after :: Time -> b -> SF a (Event b)
after t_ev x = SF {sfTF = tf0}
  where
    tf0 _ = if t_ev <= 0 then
      (sfNever, Event x)
    else
      (afterAux 0.0, NoEvent)

    afterAux t = SFTIVar {sfTF' = tf}
      where
        tf dt _ = let t' = t + dt
          in
            if t' >= t_ev then
              (sfNever, Event x)
            else
              (afterAux t', NoEvent)

-- Event source with repeated occurrences with interval dt
-- Note: If the interval is too short w.r.t. the sampling intervals,
-- the result will be that events occur at every sample. However, no more
-- than one event results from any sampling interval, thus avoiding an
-- "event backlog" should sampling become more frequent at some later
-- point in time.
repeatedly :: Time -> b -> SF a (Event b)
repeatedly p_ev x | p_ev > 0 = SF {sfTF = tf0}
  | otherwise = afrpErr "repeatedly" "Non-positive period."
  where
    tf0 _ = (repAux p_ev 0.0, NoEvent)

    repAux t_ev t = SFTIVar {sfTF' = tf}
      where
        tf dt _ = let t' = t + dt
          in
            if t' >= t_ev then
              (repAux (nextEventTime t' t_ev) t', Event x)
            else
              (repAux t_ev t', NoEvent)

        nextEventTime t t_ev =
          fromIntegral (truncate (t / p_ev) + 1) * p_ev

-- A rising edge detector. Useful for things like detecting key presses.
-- Note that we initialize the loop with state set to True so that there
-- will not be an occurrence at t0 in the logical time frame in which
-- this is started.
edge :: SF Bool (Event ())
edge = edgeBy isEdge True
  where
    isEdge False False = Nothing
    isEdge False True  = Just ()
    isEdge True  True  = Nothing
    isEdge True  False = Nothing

-- Edge detector parameterized on the edge detection function and initial
-- state, i.e., the previous input sample. The first argument to the
-- edge detection function is the previous sample, the second the current one.
edgeBy :: (a -> a -> Maybe b) -> a -> SF a (Event b)
edgeBy isEdge a_init = SF {sfTF = tf0}
  where
    tf0 a0 = (ebAux a0, maybeToEvent (isEdge a_init a0))

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    ebAux a_prev = SFTIVar {sfTF' = tf}
      where
        tf dt a = (ebAux a, maybeToEvent (isEdge a_prev a))

-- Detects an edge where a maybe signal is changing from nothing to something.
edgeJust :: SF (Maybe a) (Event a)
edgeJust = edgeBy isJustEdge (Just undefined)
  where
    isJustEdge Nothing Nothing = Nothing
    isJustEdge Nothing ma@(Just _) = ma
    isJustEdge (Just _) (Just _) = Nothing
    isJustEdge (Just _) Nothing = Nothing

-----
-- Stateful event suppression
-----

-- Suppression of initial (at local time 0) event.
notYet :: SF (Event a) (Event a)
notYet = initially NoEvent

-----
-- Collection-oriented combinators
-----

-- Spatial parallel composition of a signal function collection.
par :: Functor col => col (SF a b) -> SF a (col b)
par sfs0 = SF {sfTF = tf0}
  where
    tf0 a0 =
      let sfs0 = fmap (\sf0 -> (sfTF sf0) a0) sfs0
          sfs  = fmap fst sfs0
          bs0  = fmap snd sfs0
      in
        (parAux sfs, bs0)

-- Internal definition. Also used in parallel swithers.
parAux :: Functor col => col (SF' a b) -> SF' a (col b)
parAux sfs = SFTIVar {sfTF' = tf}
  where
    tf dt a =
      let sfs' = fmap (\sf -> (sfTF' sf) dt a) sfs
          sfs' = fmap fst sfs'
          bs   = fmap snd sfs'
      in
        (parAux sfs', bs)

-----
-- Switchers
-----

-- !!! We could detect a NeverEvent in the various switches.
-- !!! In which case we must ensure that SFConst ... NeverEvent ...
-- !!! is covered as well!!

-- Basic switch.
switch :: SF a (b, Event c) -> (c -> SF a b) -> SF a b
switch (SF {sfTF = tf10}) k = SF {sfTF = tf0}
  where
    tf0 a0 =

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case tf10 a0 of
  (sf1, (b0, NoEvent)) -> (switchAux sf1, b0)
  (_, (_, Event c0)) -> sfTF (k c0) a0

switchAux (SFConst {sfCVal = (b, NoEvent)}) = sfConst b
switchAux sf1                               = SFTTIVar {sfTF' = tf}
  where
    tf dt a =
      case (sfTF' sf1) dt a of
        (sf1', (b, NoEvent)) -> (switchAux sf1', b)
        (_, (_, Event c)) -> sfTF (k c) a

-- Switch with delayed observation.
dSwitch :: SF a (b, Event c) -> (c -> SF a b) -> SF a b
dSwitch (SF {sfTF = tf10}) k = SF {sfTF = tf0}
  where
    tf0 a0 =
      let (sf1, (b0, ec0)) = tf10 a0
          in (case ec0 of
              NoEvent -> dSwitchAux sf1
              Event c0 -> fst (sfTF (k c0) a0),
              b0)

dSwitchAux (SFConst {sfCVal = (b, NoEvent)}) = sfConst b
dSwitchAux sf1                               = SFTTIVar {sfTF' = tf}
  where
    tf dt a =
      let (sf1', (b, ec)) = (sfTF' sf1) dt a
          in (case ec of
              NoEvent -> dSwitchAux sf1'
              Event c -> fst (sfTF (k c) a),
              b)

-- "Call-with-current-continuation" switch.
kSwitch :: SF a b -> SF (a,b) (Event c) -> (SF a b -> c -> SF a b) -> SF a b
kSwitch sf10@(SF {sfTF = tf10}) (SF {sfTF = tfe0}) k = SF {sfTF = tf0}
  where
    tf0 a0 =
      let (sf1, b0) = tf10 a0
          in
            case tfe0 (a0, b0) of
              (sfe, NoEvent) -> (kSwitchAux sf1 sfe, b0)
              (_, Event c0) -> sfTF (k sf10 c0) a0

kSwitchAux sf1 (SFConst {sfCVal = NoEvent}) = sf1
kSwitchAux sf1 sfe                          = SFTTIVar {sfTF' = tf}
  where
    tf dt a =
      let (sf1', b) = (sfTF' sf1) dt a
          in
            case (sfTF' sfe) dt (a, b) of
              (sfe', NoEvent) -> (kSwitchAux sf1' sfe', b)
              (_, Event c) -> sfTF (k (freeze sf1 dt) c) a

-- kSwitch with delayed observation.
dkSwitch :: SF a b -> SF (a,b) (Event c) -> (SF a b -> c -> SF a b) -> SF a b
dkSwitch sf10@(SF {sfTF = tf10}) (SF {sfTF = tfe0}) k = SF {sfTF = tf0}
  where
    tf0 a0 =
      let (sf1, b0) = tf10 a0
          in (case tfe0 (a0, b0) of

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              (sfe, NoEvent) -> kSwitchAux sf1 sfe
              (_, Event c0) -> fst (sfTF (k sf10 c0) a0),
              b0)

kSwitchAux sf1 (SFConst {sfCVal = NoEvent}) = sf1
kSwitchAux sf1 sfe                          = SFTTIVar {sfTF' = tf}
  where
    tf dt a =
      let (sf1', b) = (sfTF' sf1) dt a
          in (case (sfTF' sfe) dt (a, b) of
              (sfe', NoEvent) -> kSwitchAux sf1' sfe'
              (_, Event c) -> fst (sfTF (k (freeze sf1 dt) c) a),
              b)

-- Recurring switch.
rSwitch :: SF a b -> SF (a, Event (SF a b)) b
rSwitch sf = switch (first sf) rSwitch'
  where
    rSwitch' sf = switch (sf *** notYet) rSwitch'

-- Recurring switch with delayed observation.
drSwitch :: SF a b -> SF (a, Event (SF a b)) b
drSwitch sf = dSwitch (first sf) drSwitch'
  where
    drSwitch' sf = dSwitch (sf *** notYet) drSwitch'

-- Parallel switch (dynamic collection of signal functions spatially composed
-- in parallel).
pSwitch :: Functor col =>
  col (SF a b) -> SF (a,col b) (Event c) -> (col (SF a b)->c-> SF a (col b))
  -> SF a (col b)
pSwitch sfs0 (SF {sfTF = tfe0}) k = SF {sfTF = tf0}
  where
    tf0 a0 =
      let sfs0 = fmap (\sf0 -> (sfTF sf0) a0) sfs0
          sfs  = fmap fst sfs0
          bs0  = fmap snd sfs0
          in
            case tfe0 (a0, bs0) of
              (sfe, NoEvent) -> (pSwitchAux sfs sfe, bs0)
              (_, Event c0) -> sfTF (k sfs0 c0) a0

pSwitchAux sfs (SFConst {sfCVal = NoEvent}) = parAux sfs
pSwitchAux sfs sfe = SFTTIVar {sfTF' = tf}
  where
    tf dt a =
      let sfs' = fmap (\sf -> (sfTF' sf) dt a) sfs
          sfs' = fmap fst sfs'
          bs   = fmap snd sfs'
          in
            case (sfTF' sfe) dt (a, bs) of
              (sfe', NoEvent) -> (pSwitchAux sfs' sfe', bs)
              (_, Event c) -> sfTF (k (freezeCol sfs dt) c) a

-- Parallel switch with delayed observation.
dpSwitch :: Functor col =>
  col (SF a b) -> SF (a,col b) (Event c) -> (col (SF a b)->c->SF a (col b))
  -> SF a (col b)
dpSwitch sfs0 (SF {sfTF = tfe0}) k = SF {sfTF = tf0}
  where
    tf0 a0 =

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let sfbs0 = fmap (\sf0 -> (sfTF sf0) a0) sfs0
    bs0   = fmap snd sfbs0
in
  (case tfe0 (a0, bs0) of
    (sfe, NoEvent) -> dpSwitchAux (fmap fst sfbs0) sfe
    (_, Event c0)  -> fst (sfTF (k sfs0 c0) a0),
    bs0)

dpSwitchAux sfs (SFConst {sfCVal = NoEvent}) = parAux sfs
dpSwitchAux sfs sfe = SFTIVar {sfTF' = tf}
  where
    tf dt a =
      let sfbs' = fmap (\sf -> (sfTF' sf) dt a) sfs
          bs    = fmap snd sfbs'
      in
        (case (sfTF' sfe) dt (a, bs) of
          (sfe', NoEvent) -> dpSwitchAux (fmap fst sfbs')
                                         sfe'
          (_, Event c)   -> fst (sfTF (k (freezeCol sfs dt)
                                         c)
                                         a),
          bs)

-- Recurring parallel switch.
-- (Unclear if possible to derive from pSwitch, but the definition would in
-- any case be complicated.)
rpSwitch :: Functor col =>
  col (SF a b) -> SF (a, Event (col (SF a b) -> col (SF a b))) (col b)
rpSwitch sfs0 = SF {sfTF = tf0}
  where
    tf0 (a0, ef0) =
      let sfs0' = case ef0 of
          NoEvent -> sfs0
          Event f0 -> f0 sfs0
          sfbs0 = fmap (\sf0 -> sfTF sf0 a0) sfs0'
          sfs   = fmap fst sfbs0
          bs0   = fmap snd sfbs0
      in
        (rpSwitchAux sfs, bs0)

rpSwitchAux sfs = SFTIVar {sfTF' = tf}
  where
    tf dt (a, ef) =
      let sfbs = case ef of
          NoEvent -> fmap (\sf -> sfTF' sf dt a) sfs
          Event f -> fmap (\sf -> sfTF sf a)
                        (f (freezeCol sfs dt))
          sfs' = fmap fst sfbs
          bs   = fmap snd sfbs
      in
        (rpSwitchAux sfs', bs)

-- Recurring parallel switch with delayed observation (aka. the DARPA switch!)
drpSwitch :: Functor col =>
  col (SF a b) -> SF (a, Event (col (SF a b) -> col (SF a b))) (col b)
drpSwitch sfs0 = SF {sfTF = tf0}
  where
    tf0 (a0, ef0) =
      let sfbs0 = fmap (\sf0 -> sfTF sf0 a0) sfs0
          bs0   = fmap snd sfbs0
      in
        (case ef0 of
          NoEvent -> drpSwitchAux (fmap fst sfbs0)

```

```

          Event f0 -> drpSwitchAux (fmap fst
                                   (fmap (\sf0 -> sfTF sf0 a0)
                                         (f0 sfs0))),
          bs0)

drpSwitchAux sfs = SFTIVar {sfTF' = tf}
  where
    tf dt (a, ef) =
      let sfbs = fmap (\sf -> sfTF' sf dt a) sfs
          bs   = fmap snd sfbs
      in
        (case ef of
          NoEvent -> drpSwitchAux (fmap fst sfbs)
          Event f ->
            let sfs' = f (freezeCol sfs dt)
            in
              drpSwitchAux (fmap fst
                            (fmap (\sf->sfTF sf a)
                                  sfs')),
          bs)

-----
-- Wave-form generation
-----

-- Zero-order hold.
hold :: a -> SF (Event a) a
hold a0 = switch (arr dup >>> first (constant a0)) hold'
  where
    hold' a = switch (constant a &&& notYet) hold'

-- Delayed zero-order hold.
-- !!! Actually, since we're switching into a stateless signal function,
-- !!! this is just (hold a0 >>> delay a0).
-- !!! So why do we have dHold???)
dHold a0 = dSwitch (arr dup >>> first (constant a0)) dHold'
  where
    dHold' a = dSwitch (constant a &&& notYet) dHold'

-- Tracks input signal when available, holds last value when disappears.
trackAndHold :: a -> SF (Maybe a) a
trackAndHold a = arr (maybe NoEvent Event) >>> hold a

-- Similar to trackAndHold, but using a delayed hold:
-- !!! Actually, this is just (trackAndHold a0 >>> delay a0).
dTrackAndHold :: a -> SF (Maybe a) a
dTrackAndHold a = arr (maybe NoEvent Event) >>> dHold a

-----
-- Accumulators
-----

accum :: a -> SF (Event (a -> a)) (Event a)
accum = accumBy (flip ($))

-- Identity: accumBy f = accumFilter (\b a -> let b' = f b a in (b',Just b'))
accumBy :: (b -> a -> b) -> b -> SF (Event a) (Event b)
accumBy f b_init = SF {sfTF = tf0}
  where

```

```

tf0 NoEvent = (abAux b_init, NoEvent)
tf0 (Event a0) = let b' = f b_init a0
                 in (abAux b', Event b')

abAux b = SFTIVar {sfTF' = tf}
  where
    tf _ NoEvent = (abAux b, NoEvent)
    tf _ (Event a) = let b' = f b a
                     in (abAux b', Event b')

accumFilter :: (c -> a -> (c, Maybe b)) -> c -> SF (Event a) (Event b)
accumFilter f c_init = SF {sfTF = tf0}
  where
    tf0 NoEvent = (afAux c_init, NoEvent)
    tf0 (Event a0) = case f c_init a0 of
      (c', Nothing) -> (afAux c', NoEvent)
      (c', Just b0) -> (afAux c', Event b0)

afAux c = SFTIVar {sfTF' = tf}
  where
    tf _ NoEvent = (afAux c, NoEvent)
    tf _ (Event a) = case f c a of
      (c', Nothing) -> (afAux c', NoEvent)
      (c', Just b) -> (afAux c', Event b)

count :: Integral b => SF (Event a) (Event b)
count = accumBy (\n _ -> n + 1) 0

-----

-- Delay
-----

-- Consider changing name to pre?
delay :: a -> SF a a
delay a_init = SF {sfTF = tf0}
  where
    tf0 a0 = (delayAux a0, a_init)

    delayAux a_prev = SFTIVar {sfTF' = tf}
      where
        tf dt a = (delayAux a, a_prev)

-----

-- Integral
-----

-- Integration using the rectangle rule.
integral :: Fractional a => SF a a
integral = SF {sfTF = tf0}
  where
    igr10 = 0.0

    tf0 a0 = (integralAux igr10 a0, igr10)

    integralAux igr1 a_prev = SFTIVar {sfTF' = tf}
      where
        tf dt a = (integralAux igr1' a, igr1')
          where
            igr1' = igr1 + a_prev * realToFrac dt

```

```

-----
-- Loops with guaranteed well-defined feedback
-----

loopDelay :: c -> SF (a,c) (b,c) -> SF a b
loopDelay = undefined

loopIntegral :: Fractional c => SF (a,c) (b,c) -> SF a b
loopIntegral = undefined

-----

-- Reactimation
-----

-- Reactimation of a signal function.
-- init ..... IO action for initialization. Will only be invoked once,
--             at (logical) time 0, before first call to "sense".
--             Expected to return the value of input at time 0.
-- sense ..... IO action for sensing of system input.
--             arg. #1 ..... True: action may block, waiting for an OS event.
--                             False: action must not block.
--             res. #1 ..... Time interval since previous invocation of the sensing
--                             action (or, the first time round, the init action),
--                             returned. The interval must be _strictly_ greater
--                             than 0. Thus even a non-blocking invocation must
--                             ensure that time progresses.
--             res. #2 ..... Nothing: input is unchanged w.r.t. the previously
--                             returned input sample.
--                             Just i: the input is currently i.
--                             It is OK to always return "Just", even if input is
--                             unchanged.
-- actuate .... IO action for outputting the system output.
--             arg. #1 ..... True: output may have changed from previous output
--                             sample.
--                             False: output is definitely unchanged from previous
--                             output sample.
--                             It is OK to ignore argument #1 and assume that the
--                             the output has always changed.
--             arg. #2 ..... Current output sample.
--             result ..... Termination flag. Once True, reactimate will exit
--                             the reactimation loop and return to its caller.
-- sf ..... Signal function to reactimate.

reactimate :: IO a
            -> (Bool -> IO (DTime, Maybe a))
            -> (Bool -> b -> IO Bool)
            -> SF a b
            -> IO ()

reactimate init sense actuate (SF {sfTF = tf0}) =
  do
    a0 <- init
    let (sf, b0) = tf0 a0
        loop sf a0 b0
    where
      loop sf a b = do
        done <- actuate True b
        unless (a `seq` b `seq` done) $ do
          (dt, ma') <- sense False
          let a' = maybe a id ma'
              (sf', b') = (sfTF' sf) dt a'
          loop sf' a' b'

```

